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*What is it ye would see?
If aught of woe or wonder, cease your search.
— Horatio in Hamlet, Act V, scene II*